

# Grundlegende Parsingalgorithmen

## Tomita-Parser

Kurt Eberle

k.eberle@lingenio.de

(Viele Folien, Teile von Folien, Materialien von **Helmut Schmid's**  
Parsing-Kurs WS14 Tübingen, u.a.)

01. August, 2018

# Überblick

Idee und Hintergrund

Daten-Strukturen

Tomita Erkenner

Tomita-Erkenner: Operationen

Parse-Wald

# Überblick

Idee und Hintergrund

Daten-Strukturen

Tomita Erkenner

Tomita-Erkenner: Operationen

Parse-Wald

## Tomita Parser

- ▶ *An efficient all-paths parsing algorithm for natural languages*  
(Masaru Tomita, 1984)

## Tomita Parser

- ▶ *An efficient all-paths parsing algorithm for natural languages*  
(Masaru Tomita, 1984)
- ▶ Other name: GLR parser (generalized LR)

## Tomita Parser

- ▶ *An efficient all-paths parsing algorithm for natural languages* (Masaru Tomita, 1984)
- ▶ Other name: GLR parser (generalized LR)
- ▶ Problem: Many grammars are not in LR(k). How can we nevertheless use an LR parser?

## Tomita Parser

- ▶ *An efficient all-paths parsing algorithm for natural languages* (Masaru Tomita, 1984)
- ▶ Other name: GLR parser (generalized LR)
- ▶ Problem: Many grammars are not in LR( $k$ ). How can we nevertheless use an LR parser?
- ▶ Idea 1: Backtracking

## Tomita Parser

- ▶ *An efficient all-paths parsing algorithm for natural languages*  
(Masaru Tomita, 1984)
- ▶ Other name: GLR parser (generalized LR)
- ▶ Problem: Many grammars are not in LR( $k$ ). How can we nevertheless use an LR parser?
- ▶ Idea 1: Backtracking
- ▶ Idea 2: Parallel Simulation of multiple LR parsers  
Non-determinism is handled by

## Tomita Parser

- ▶ *An efficient all-paths parsing algorithm for natural languages*  
(Masaru Tomita, 1984)
- ▶ Other name: GLR parser (generalized LR)
- ▶ Problem: Many grammars are not in LR( $k$ ). How can we nevertheless use an LR parser?
- ▶ Idea 1: Backtracking
- ▶ Idea 2: Parallel Simulation of multiple LR parsers  
Non-determinism is handled by
  - ▶ Reduplication of the parser

## Tomita Parser

- ▶ *An efficient all-paths parsing algorithm for natural languages* (Masaru Tomita, 1984)
- ▶ Other name: GLR parser (generalized LR)
- ▶ Problem: Many grammars are not in LR( $k$ ). How can we nevertheless use an LR parser?
- ▶ Idea 1: Backtracking
- ▶ Idea 2: Parallel Simulation of multiple LR parsers  
Non-determinism is handled by
  - ▶ Reduplication of the parser
  - ▶ Tree-structured stack (for left-hand side of the configuration)

## Tomita Parser

- ▶ *An efficient all-paths parsing algorithm for natural languages* (Masaru Tomita, 1984)
- ▶ Other name: GLR parser (generalized LR)
- ▶ Problem: Many grammars are not in LR( $k$ ). How can we nevertheless use an LR parser?
- ▶ Idea 1: Backtracking
- ▶ Idea 2: Parallel Simulation of multiple LR parsers  
Non-determinism is handled by
  - ▶ Reduplication of the parser
  - ▶ Tree-structured stack (for left-hand side of the configuration)
  - ▶ Graph-structured stack

## Tomita Parser

- ▶ *An efficient all-paths parsing algorithm for natural languages* (Masaru Tomita, 1984)
- ▶ Other name: GLR parser (generalized LR)
- ▶ Problem: Many grammars are not in LR( $k$ ). How can we nevertheless use an LR parser?
- ▶ Idea 1: Backtracking
- ▶ Idea 2: Parallel Simulation of multiple LR parsers  
Non-determinism is handled by
  - ▶ Reduplication of the parser
  - ▶ Tree-structured stack (for left-hand side of the configuration)
  - ▶ Graph-structured stack
- ▶ Graph-structured stack:

## Tomita Parser

- ▶ *An efficient all-paths parsing algorithm for natural languages* (Masaru Tomita, 1984)
- ▶ Other name: GLR parser (generalized LR)
- ▶ Problem: Many grammars are not in LR( $k$ ). How can we nevertheless use an LR parser?
- ▶ Idea 1: Backtracking
- ▶ Idea 2: Parallel Simulation of multiple LR parsers  
Non-determinism is handled by
  - ▶ Reduplication of the parser
  - ▶ Tree-structured stack (for left-hand side of the configuration)
  - ▶ Graph-structured stack
- ▶ Graph-structured stack:
  - ▶ Directed, acyclic graph with a single source node

## Tomita Parser

- ▶ *An efficient all-paths parsing algorithm for natural languages* (Masaru Tomita, 1984)
- ▶ Other name: GLR parser (generalized LR)
- ▶ Problem: Many grammars are not in LR( $k$ ). How can we nevertheless use an LR parser?
- ▶ Idea 1: Backtracking
- ▶ Idea 2: Parallel Simulation of multiple LR parsers  
Non-determinism is handled by
  - ▶ Reduplication of the parser
  - ▶ Tree-structured stack (for left-hand side of the configuration)
  - ▶ Graph-structured stack
- ▶ Graph-structured stack:
  - ▶ Directed, acyclic graph with a single source node
  - ▶ Nodes correspond to parser configurations.

## Tomita Parser

- ▶ *An efficient all-paths parsing algorithm for natural languages* (Masaru Tomita, 1984)
- ▶ Other name: GLR parser (generalized LR)
- ▶ Problem: Many grammars are not in LR( $k$ ). How can we nevertheless use an LR parser?
- ▶ Idea 1: Backtracking
- ▶ Idea 2: Parallel Simulation of multiple LR parsers  
Non-determinism is handled by
  - ▶ Reduplication of the parser
  - ▶ Tree-structured stack (for left-hand side of the configuration)
  - ▶ Graph-structured stack
- ▶ Graph-structured stack:
  - ▶ Directed, acyclic graph with a single source node
  - ▶ Nodes correspond to parser configurations.
  - ▶ The end nodes are the active configurations.

# Eine ambige Grammatik

PP Attachment? S oder NP

- ```
-----  
 (1) S --> NP VP  
 (2) S --> S PP  
 (3) NP --> *n  
 (4) NP --> *det *n  
 (5) NP --> NP PP  
 (6) PP --> *prep NP  
 (7) VP --> *v NP  
-----
```

**Figure 2-5:** An Example Ambiguous Grammar

# Tabelle der Grammatik

PP Attachment? Shift oder Reduce

Figure 2-5: An Example Ambiguous Grammar

| State | *det | *n   | *v  | *prep   | \$  | NP | PP | VP | S |
|-------|------|------|-----|---------|-----|----|----|----|---|
| 0     | sh3  | sh4  |     |         |     | 2  |    |    | 1 |
| 1     |      |      |     | sh6     | acc |    | 5  |    |   |
| 2     |      |      | sh7 | sh6     |     |    | 9  | 8  |   |
| 3     |      | sh10 |     |         |     |    |    |    |   |
| 4     |      |      | re3 | re3     | re3 |    |    |    |   |
| 5     |      |      |     | re2     | re2 |    |    |    |   |
| 6     | sh3  | sh4  |     |         |     |    | 11 |    |   |
| 7     | sh3  | sh4  |     |         |     |    | 12 |    |   |
| 8     |      |      |     | re1     | re1 |    |    |    |   |
| 9     |      |      | re6 | re6     | re6 |    |    |    |   |
| 10    |      |      | re4 | re4     | re4 |    |    |    |   |
| 11    |      |      | re8 | re6,sh8 | re6 |    | 9  |    |   |
| 12    |      |      |     | re7,sh8 | re7 |    |    | 9  |   |

Figure 2-6: LR Parsing Table with Multiple Entries

## Stack als Liste

I saw a man on the bed in the apartment **with** a telescope

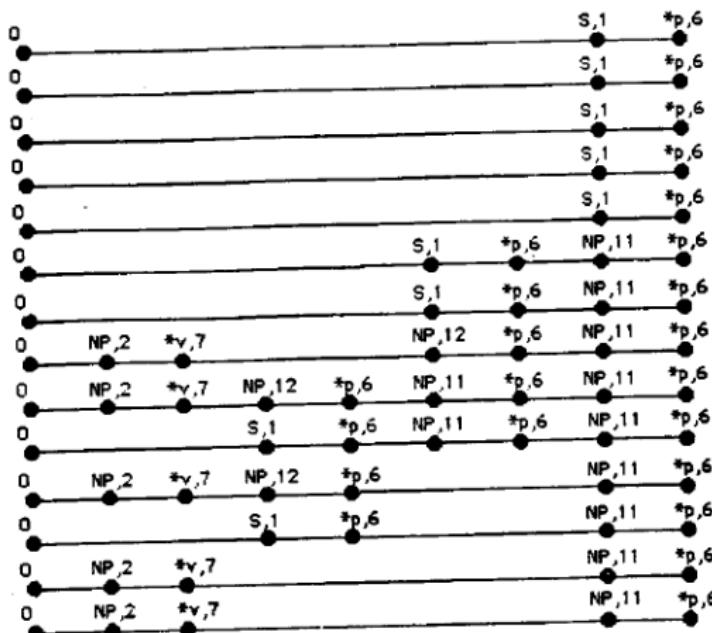


Figure 3-1: Stack List

## Stack strukturiert als Baum

I saw a man on the bed in the apartment **with** a telescope

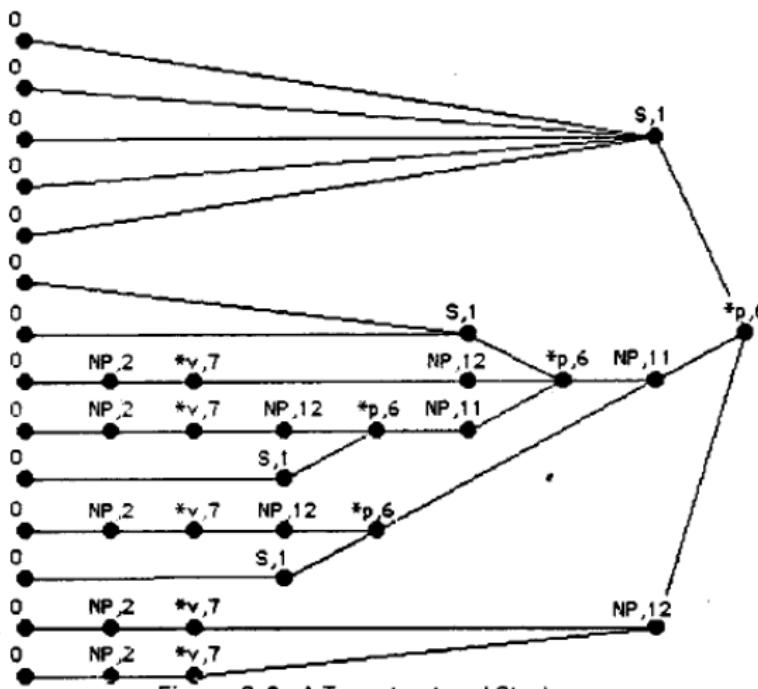


Figure 3-2: A Tree-structured Stack

## Stack strukturiert als Graph

I saw a man on the bed in the apartment **with** a telescope

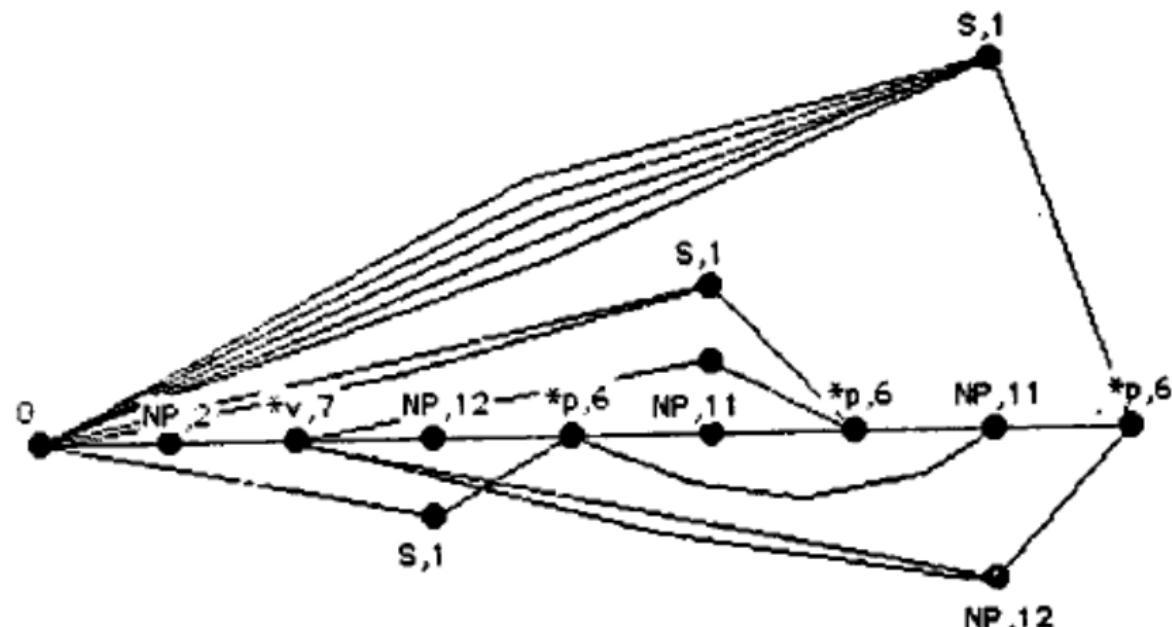


Figure 3-3: A Graph-Structured Stack

# Überblick

Idee und Hintergrund

Daten-Strukturen

Tomita Erkenner

Tomita-Erkenner: Operationen

Parse-Wald

## Tomita Erkenner: Daten-Strukturen

- ▶  $\{a, b, c\}$ : Set containing the elements  $a, b$  and  $c$ .
- ▶  $[a, b, c]$ : List containing the elements  $a, b$  and  $c$ .
- ▶  $\circ$ : Concatenation operator for lists
- ▶  $U_i$ : Set of top-most stack nodes after  $i$  input symbols have been processed
- ▶  $\langle i, s, l \rangle$ : a node of the graph-structured stack
- ▶  $\langle 0, s_0, \{\} \rangle$ : Root of the stack
- ▶  $Actions(s, x)$ : Set of actions in state  $s$  with look-ahead symbol  $x$
- ▶  $Goto(s, D)$ : New state after the non-terminal  $D$  has been consumed in state  $s$

# Überblick

Idee und Hintergrund

Daten-Strukturen

Tomita Erkenner

Tomita-Erkenner: Operationen

Parse-Wald

# Tomita Erkenner

Recognizer( $x_1 \dots x_n$ )

```

 $x_{n+1} := \$$           %%Add end symbol to input string
 $U_0 := [\langle 0, S_0, \{\} \rangle]$  %%initial stack element with start configuration
For  $i := 1$  to  $n + 1$ 
     $U_i := []$            %%position- $i$  stack elements
     $P := []$             %%nodes already considered
    For all  $v = \langle i - 1, s, l \rangle$  such that  $v \in U_{i-1}$  from left to right
         $P := P \circ [v]$ 
        For all  $a \in Actions(s, x_i)$ 
            If  $a = shift\ s'$  then
                Shift( $v, s', i$ )
            else if  $a = reduce\ p$  then
                Reduce( $v, p, i$ )
            else if  $a = accept$  then
                accept
            If  $U_i = []$  then
                Report error
        Accept
    
```

# Überblick

Idee und Hintergrund

Daten-Strukturen

Tomita Erkenner

Tomita-Erkenner: Operationen

Parse-Wald

# Tomita-Erkenner: Shift

Shift( $v, s, i$ )

If  $\exists v' = \langle i, s, l \rangle$  such that  $v' \in U_i$  then

$l := l \cup \{v\}$

else

$U_i := U_i \circ [\langle i, s, \{v\} \rangle]$

# Tomita-Erkenner: Predecessor

Predecessor( $v = \langle j, s, l \rangle, k$ )

```
If  $k = 0$  then
    return {v}
else
    return  $\cup_{v' \in I} predecessor(v', k - 1)$ 
```

# Tomita-Erkenner: Reduce

Reduce( $v, p, i$ )

For all  $v'_1 = \langle j', s', l'_1 \rangle$  such that  $v'_1 \in \text{Predecessor}(v, |p|)$

$s'' := \text{Goto}(s', D_p)$

If  $\exists v'' = \langle i - 1, s'', l'' \rangle$  such that  $v'' \in U_{i-1}$

then If  $v'_1 \in l''$

then do nothing

else if  $\exists v'_2 = \langle j'', s', l'_2 \rangle$  such that  $v'_2 \in l''$

then  $v''_c := \langle i - 1, s'', \{v'_1\} \rangle$

For all 'reduce  $p'$   $\in \text{Actions}(s'', x_i)$

$\text{Reduce}(v''_c, p, i)$

else  $l'' := l'' \cup \{v'_1\}$

If  $v'' \in P$  then  $v''_c := \langle i - 1, s'', \{v'_1\} \rangle$

For all 'reduce  $p'$   $\in \text{Actions}(s'', x_i)$

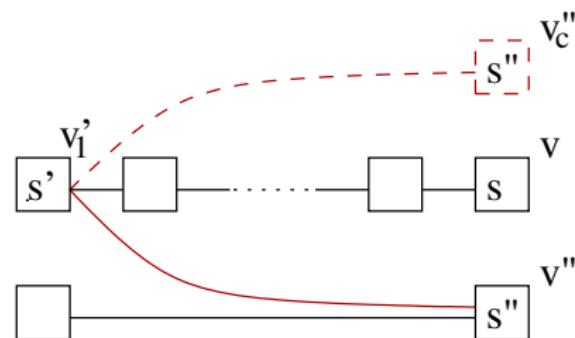
$\text{Reduce}(v''_c, p, i)$

else

$U_{i-1} := U_{i-1} \circ [\langle i - 1, s'', \{v'_1\} \rangle]$

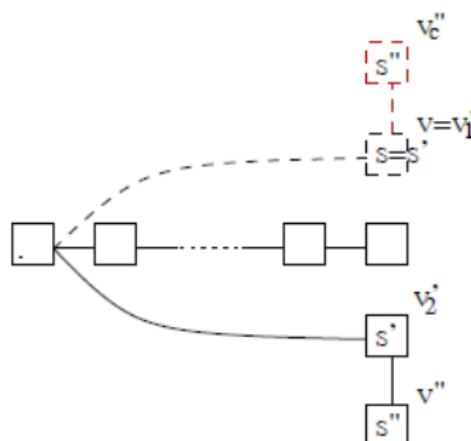
# Tomita-Erkenner: Kopien

no  $s'$  predecessor yet included,  $v''$  already in P ...



## Tomita-Erkenner: Kopien

$s'$  predecessor already included ( $v''$  already in P) ...



## Beispiel: Stacks teilen und zusammenführen

$F \rightarrow D E$

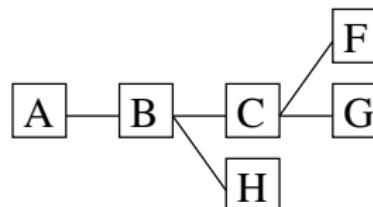
Auszug aus einer Grammatik ...  $G \rightarrow D E$

$H \rightarrow C D E$

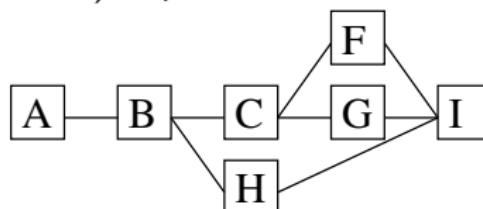
Parsing-Situation...



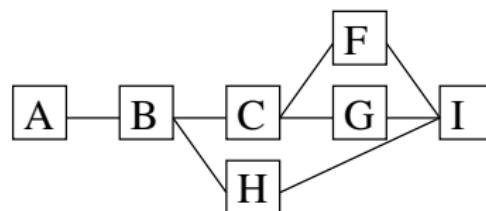
Drei Reduktionen...



Shift wird auf alle (offenen) Top-Elemente des Stacks angewendet

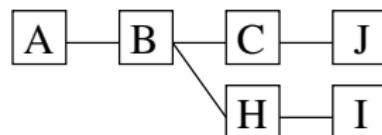


## Beispiel: Stacks teilen und zusammenführen



Lokale Ambiguität...

$J \rightarrow F I$   
 $J \rightarrow G I$



## Beispiel

(Grammatik und Zustände von "ABgram.pdf")

|   |   |    |                                                                                                                                                                                         |
|---|---|----|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 2 | a | U2 | $[\langle 2,s3, \{v12\} \rangle_{Aa}, \langle 2,s5, \{v13\} \rangle_{Ba}, \langle 2,s6, \{v12\} \rangle_{AB},$<br>$\langle 2,s7, \{v13\} \rangle_{BA}, \langle 2,s8, \{v0\} \rangle_s]$ |
| 1 | a | U1 | $[v11\langle 1,s1, \{v0\} \rangle_a, v12\langle 1,s2, \{v0\} \rangle_A, v13\langle 1,s4, \{v0\} \rangle_B]$                                                                             |
| 0 | 0 | U0 | $[v0\langle 0,so, \{\} \rangle]$                                                                                                                                                        |

# Kontroll-Tabelle Beispiel

## Grammar

1:  $S \rightarrow NP\ VP$

2:  $VP \rightarrow VP\ PP$

3:  $VP \rightarrow v\ NP$

4:  $PP \rightarrow p\ NP$

5:  $NP \rightarrow NP\ PP$

6:  $NP \rightarrow d\ N1$

7:  $NP \rightarrow N1$

8:  $N1 \rightarrow a\ N1$

9:  $N1 \rightarrow n$

# Kontroll-Tabelle Beispiel

Table

|    | d  | a  | n  | p      | v   | \$  | N1 | NP | PP | VP | S |
|----|----|----|----|--------|-----|-----|----|----|----|----|---|
| 0  | s9 | s5 | s4 |        |     |     | 8  | 2  |    |    | 1 |
| 1  |    |    |    |        |     | acc |    |    |    |    |   |
| 2  |    |    |    | s12    | s14 |     |    |    | 3  | 10 |   |
| 3  |    |    |    | r5     | r5  | r5  |    |    |    |    |   |
| 4  |    |    |    | r9     | r9  | r9  |    |    |    |    |   |
| 5  |    | s5 | s4 |        |     |     | 6  |    |    |    |   |
| 6  |    |    |    | r8     | r8  | r8  |    |    |    |    |   |
| 7  |    |    |    | r6     | r6  | r6  |    |    |    |    |   |
| 8  |    |    |    | r7     | r7  | r7  |    |    |    |    |   |
| 9  |    | s5 | s4 |        |     |     | 7  |    |    |    |   |
| 10 |    |    |    | s12    |     | r1  |    |    | 11 |    |   |
| 11 |    |    |    | r2     |     | r2  |    |    |    |    |   |
| 12 | s9 | s5 | s4 |        |     |     | 8  | 13 |    |    |   |
| 13 |    |    |    | r4/s12 | r4  | r4  |    |    | 3  |    |   |
| 14 | s9 | s5 | s4 |        |     |     | 8  | 15 |    |    |   |
| 15 |    |    |    | r3/s12 |     | r3  |    |    | 3  |    |   |

# Überblick

Idee und Hintergrund

Daten-Strukturen

Tomita Erkenner

Tomita-Erkenner: Operationen

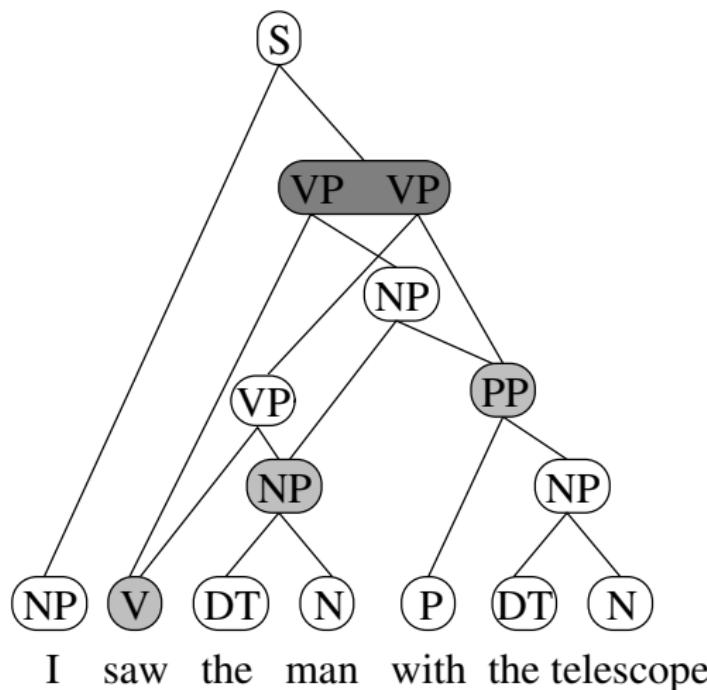
Parse-Wald

## Parse-Wald

- ▶ Problem: Sätze können exponentiell viele Analysen haben  
⇒ Output der Analysen hat exponentielle Laufzeit
- ▶ Lösung: Kompakte Repräsentation in der Form eines *Parse-Waldes*
- ▶ Parse-Wald:
  - ▶ Gerichteter Graph mit eindeutigem Wurzelknoten
  - ▶ Teilbäume werden in verschiedenen Analysen benutzt (⇒ Graph)
  - ▶ Parse-Bäume die sich nur in einem einzigen Teilbaum (über demselben Teilstring) unterscheiden werden zusammengefasst und die Top-Knoten der Teilbäume werden in einem *gepackten Knoten* (*packed node*) zusammengeführt.
- ▶ Extraktion der individuellen Analysem mit Backtracking

# Parse-Wald

with packed nodes and shared nodes



# Parse-Wald

with and-nodes and or-nodes (dotted lines)

