

# Graph-Based Methods in Coreference Resolution

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# Structure of the report

- Introduction to coreference
- Build anaphoricity in graph for coreference resolution
- BestCut-method based on min-cut algorithm
- An one step solution: hypergraph in coreference resolution
- Compare the methods

What is coreference?

- **Entity:** an object or a set of objects in the real world.
- **Mention:** a textual reference to an entity
- **Coreference:** more mentions in language refer to the same entity
- **Eg:** Mary has a brother John, the boy is younger than the girl

**entities:** MARY, JOHN

**mentions:** Mary, a brother, John, the boy, the girl

**coreference set:** {Mary, the girl}, {a brother, John, the boy}

# Anaphoricity

**Eg:** Mary has a brother John, the boy is younger than the girl

**anaphoric:** John, the boy, the girl

**nonanaphoric:** Mary, a brother

**Eg:** To repair the house will cost **a lot of money**

## Two step methods

**Eg:** Mary has a brother John, the boy is younger than the girl

- **classification phase:** pair of mentions based on feature sets
  - features:** e.g the distance, string match feature. etc
  - methods:** decision trees, maximum entropy classifiers
- Eg:** (Mary, a brother), (a brother, John). etc
- **clusterization phase:** to decide the entities(mentions that are coreferent)

Methods for clustering:

- locally optimized clustering
- globally optimized clustering.  
Bell tree, ILP, graph algorithms

**anaphoricity classifier:** the probability if a mention is anaphoric or not

## the results of coreference classification/anaphoricity classification

- $P_C(m_i, m_j)$ , the probability that mentions  $m_i$  and  $m_j$  are coreferent
- $P_A(m_i)$ , the probability that mention  $m_i$  is anaphoric
- $1 - P_A(m_i)$ , the probability that mention  $m_i$  is nonanaphoric

## Construction of the graph– add anaphoricity

- create the source vertex  $s$ : ANAPHORIC
- create the sink vertex  $t$ : NON ANAPHORIC
- for each mention  $m_i$ ; create one vertex  $i$
- two edges  $si$  and  $it$
- the weight of  $si$   $w_{si}$  is  $P_A(m_i)$ , i.e the probability that  $m_i$  is anaphoric
- the weight of  $it$   $w_{it}$  is  $1 - P_A(m_i)$ , i.e the probability that  $m_i$  is nonanaphoric

## minimum s-t cut:

- assign any node(mention)  $i$  with  $w_{si} > 0.5$ ,i.e  $P_A(m_i) > 0.5$  to  $s$
- assign any node  $i$  with  $w_{it} > 0.5$ ,i.e  $P_A(m_i) < 0.5$  to  $t$
- remained nodes are assigned to one of  $s$  and  $t$ .

**notice:** 0.5 as threshold is too conservative,  
i.e too fewer mentions are classified as anaphoric

In this system,  $P_A$  is rearranged so that the decision for anaphor is not too conservative

- add one edge for every mention pair  $(m_i, m_j)$  (except  $s$  and  $t$  in the graph)
- the weight of edge between  $m_i$  and  $m_j$ ,  $w_{i,j}$  is  $P_C(m_i, m_j)$

same as  $P_A$ , the weight here is also rearranged by learning to get the better result.

# minimum cut of the graph

the costs of the minimum  $s - t$  cut is:

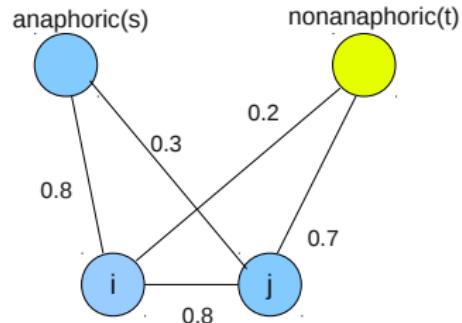
$$\min \sum_{m_i \in S - s, m_j \in T - t} w_{ij} + \sum_{m \in S} w_{mt} + \sum_{n \in T} w_{sn}$$

**Eg:** two mentions  $m_i, m_j$

$$w_{ji} = w_{ij} = 0.8$$

$$w_{si} = 0.8, w_{it} = 0.2$$

$$w_{sj} = 0.3, w_{jt} = 0.7$$



Problem with the algorithm above: tend to classify **all mentions** of a coreference as anaphoric!  
including **the first mention of an entity**.

**Can we change the graph to be a directed graph?**

- from anaphoric node to mention node
- from mention node to nonanaphoric node
- from mention node with smaller index to mention node with bigger index node

# Add direction in the graph

**Mary<sub>1</sub> has a brother<sub>2</sub> John<sub>3</sub>**

consider mentions  $m_2, m_3$

$$w_{23} = w_{32} = 0.8$$

$$w_{s3} = 0.8, w_{3t} = 0.2$$

$$w_{s2} = 0.3, w_{2t} = 0.7$$

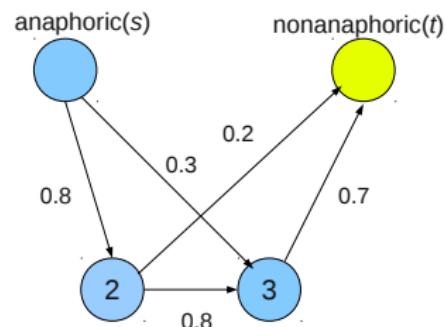
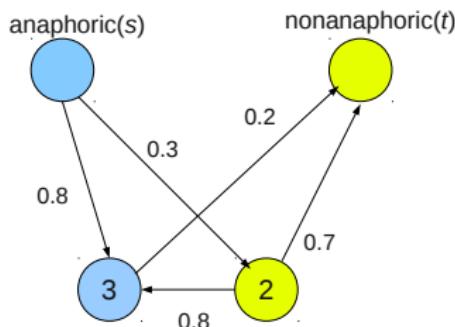
**the brother<sub>1</sub> John<sub>2</sub> is a student<sub>3</sub>**

consider mentions  $m_2, m_3$

$$w_{23} = w_{32} = 0.8$$

$$w_{s3} = 0.3, w_{3t} = 0.7$$

$$w_{s2} = 0.8, w_{2t} = 0.2$$



## Baselines unter MUC-Score and CEAF-Score

- Berger(96), et al, no anaphoricity
- Ng(2004), where  $P_A$  and  $P_C$  are not coordinated
- Luo(2007), a heuristic search on Bell tree
- D&B(2007), Integer Linear Programming with anaphoricity as constraints(hard constraints)
- F&M(2008), ILP, with transitivity as hard constraints

## Conclusion:

Large gain in precision

Small drop in recall

Improvement of F-score.

## Construction of weighted undirected graphs

- **Mention Detection:** 6 entity types  
PERSON, ORGANIZATION, LOCATION, FACILITY, GPE, UNK
- **classification:**  $P_C(m_i, m_j)$ , the probability that mention  $m_i$  and  $m_j$  are coreferent
- **Number of Graphs:** for every entity type, a graph will be constructed(6 graphs)  
the mentions from different type will not be coreferent
- **vertex:** every mention in the type is a vertex
- **edge:** the weight between two vertexes  $m_i, m_j$ (two mentions) is  $P_C(m_i, m_j)$

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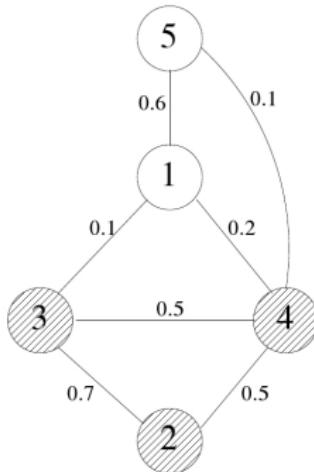
# Construction of the graphs: an example

**Mary**<sub>1</sub> has a **brother**<sub>2</sub> **John**<sub>3</sub>. **The boy**<sub>4</sub> is older than **the girl**<sub>5</sub>

5 mentions

entity type: PERSON

Only one graph will be constructed.



# When to stop the cut?

$G$ : current graph.

$S, T$ : the two parts after cut

$S.V, T.V$ : the vertexes in the two parts.  $|S.V| \geq |T.V|$

$S.E, T.E$ : the edges in the two parts

$C.E$ : the edges crossing the cut

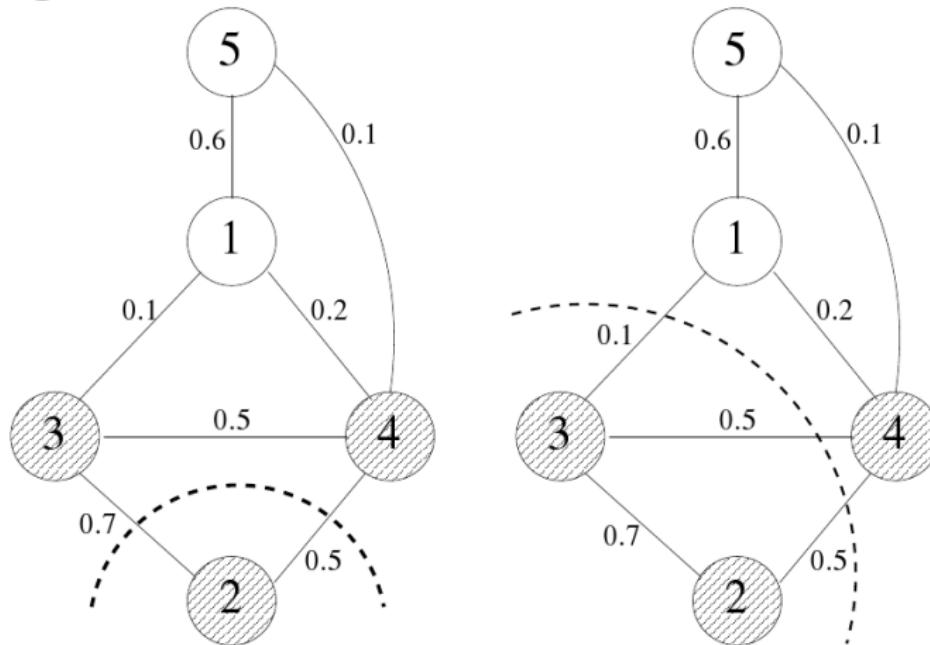
## Stop the cut or continue?

Features for stopping the cut

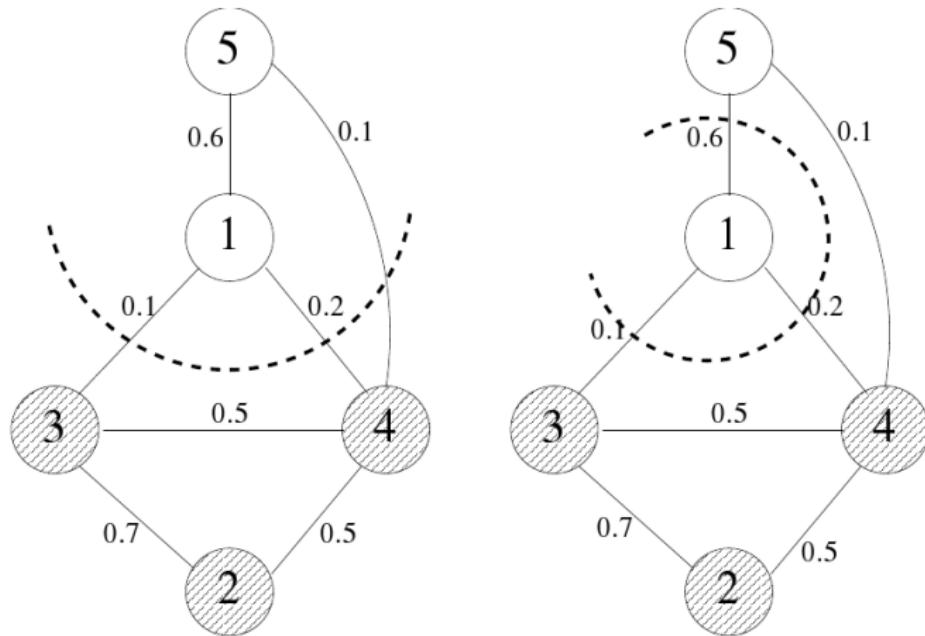
- $|S.V|/|T.V|$
- $|C.E|/|G.E|$
- $\max(C.E), \min(C.E), \text{avg}(C.E)$
- etc

# Procedure of a Cut

a sequence of s-t cuts, and the BestCut is one of them  
Eg:



# Procedure of a cut

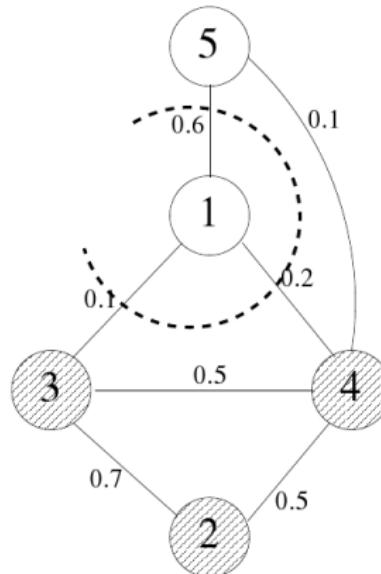


# How to choose the BestCut

Scoring a cut (s-t cut from the above procedure)

- average weight to decide if a vertex belongs to its group.
- maximum weight to decide if a vertex belongs to its group.

Eg:



evaluated under EMC-F Score and MUC P, R, F Scores  
compared with two baselines: Belltree(Luo 04) and Link-Best

- outperform the baselines with true mentions and detected mentions (If the entity types are known).
- for undetected mentions it works not so well

**Conclusion:** the mention detections and the decision of entity types are important for this algorithm

The procedure of this system:

- learn the hyperedge weights
- create a hypergraph
- partition the hypergraph in to subhypergraphs so that each subhypergraphs represents an entity

## Features used to construct the hypergraph

- StrMatch\_Npron, StrMatch\_Pron
- Alias
- Appositive
- distance, etc

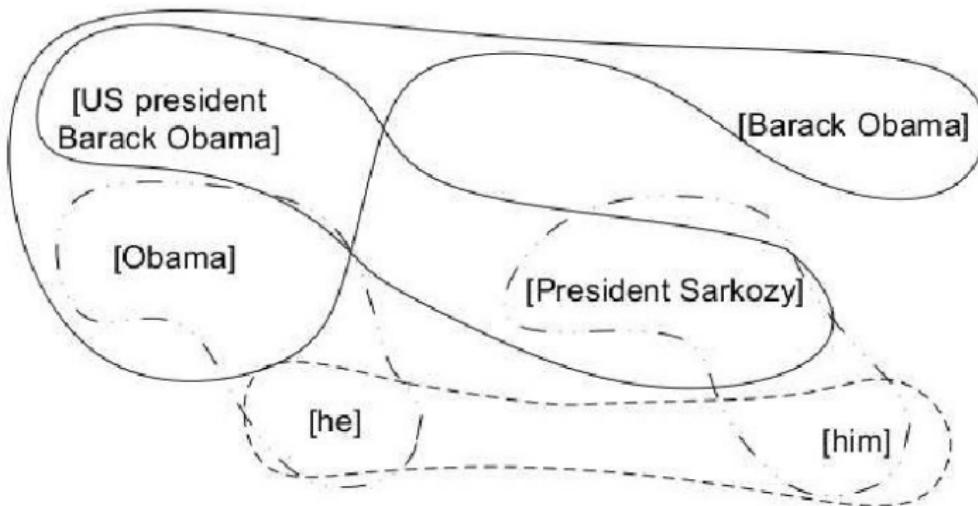
Training result for hyperedge weight:

Edge Name	Weight
Alias	0.777
StrMatch_Pron	0.702
Appositive	0.568
StrMatch_Npron	0.657
ContinuousDistAgree	0.403

## An example

**US President Barack Obama** came to Toronto today.  
**Obama** discussed the nancial crisis with **President Sarkozy**  
**He** talked to **him** about the recent downturn of the European markets.  
**Barack Obama** will leave Toronto tomorrow.

**2 entities:** BALACK OBAMA  
NICOLAS SARKOZY



*partial string match:*

{US President Barack Obama, Obama, Barack Obama}

{US President Barack Obama, President Sarkozy}

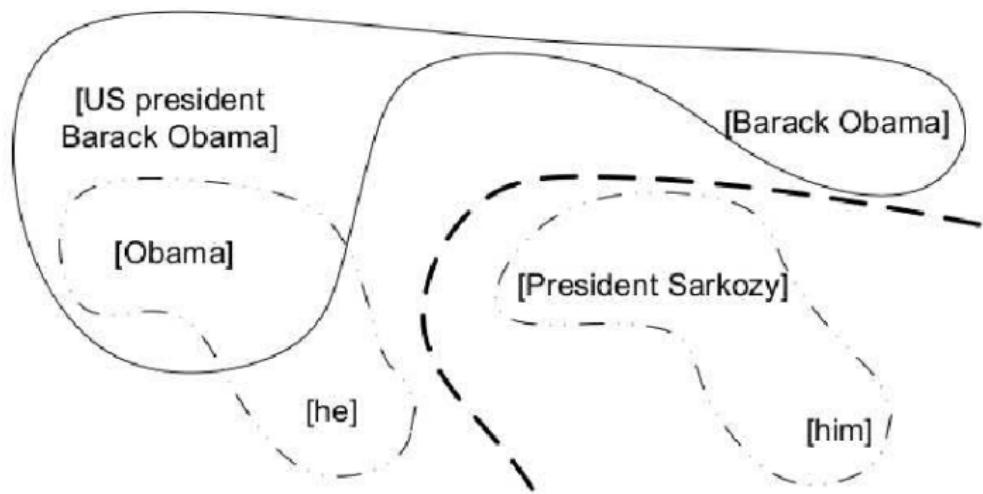
*pronoun match:* {he, him}

*all speak:* {Obama, he}

{President Sarkozy, him}

# partition of the hypergraph

- recursive 2-way partitioning
- flat-K partitioning



Using  $MUC$ ,  $B_{sys}^3$ ,  $CEAF_{sys}$  Scores

Baselines: SOON(2001)-BART(2008)

B&R(2008), 'the best performance on ACE2004'

## Conclusion:

gain in recall

drop in precision

better F-Measure than B& R in most of the cases.

# compare the 3 methods

- how many steps?

**Bestcut:** 2 steps, classification, and clustering

**s-t cut:** 3 steps, classification ( $P_A, P_C$ ), anaphoricity determination(s-t cut), coreference clustering

**Hypergraph:** 1 step, construct hypergraph based on features, and cut(spectral clustering)

- the emphasis(new idea) of the 3 methods

**Bestcut:** mincut in coreference clustering

**s-t cut:** combine anaphoricity and coreference in graph

**hypergraph:** all in one, no separation between 'classification' and clustering

- Cristina Nicolae, Gabriel Nicolae: BESTCUT: A Graph Algorithm for Coreference Resolution. EMNLP 2006:275-283
- Vincent Ng: Graph-Cut-Based Anaphoricity Determination for Coreference Resolution. HLT-NAACL 2009: 575-583
- Cai, Jie; Strube, Michael (2010). End-to-End Coreference Resolution via Hypergraph Partitioning In: COLING '10, pp.143-151

The end ;-)